

## COMPUTER MODEL OF THREE PHASE MOTOR

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*The proposed paper presents a model of an induction motor. It calculates two flux linkage – in rotor  $\Psi_r$  and in the stator  $\Psi_s$ , electromagnetic torque  $M_m$ , frequency of rotation  $\omega_r$  and the sliding -  $s$  on the base of other known parameters such as the inductance in rotor  $L_r$  and in stator  $L_s$ , the mutually inductance  $L_m$ , the active resistance in the stator  $R_s$ , the number of pole pairs  $Z_p$  and the moment values of the voltages and the currents from two of the phases supply. The present work is based on fundamental moments from the theory of the electromotion. The model is designed to accomplish the system for regulation of an induction motor by the orientation of the magnetic field. The development is made with the help of MATLAB (SIMULINK). The investigations are made with the parameters of real motor and the results are shown in a graphic form.*

It is known that the dynamics of the machine are generally described by four equations of the electric balance in the circuits of the stator and the rotor [2] :

$$(1) U_{s\alpha} = R_s \cdot i_{s\alpha} + \frac{d\Psi_{s\alpha}}{dt}$$

$$(2) U_{s\beta} = R_s \cdot i_{s\beta} + \frac{d\Psi_{s\beta}}{dt}$$

$$(3) 0 = R_r \cdot i_{r\alpha} + \frac{d\Psi_{r\alpha}}{dt}$$

$$(4) 0 = R_r \cdot i_{r\beta} + \frac{d\Psi_{r\beta}}{dt} ,$$

The symbols are as follows:

$U_{s\alpha}$  and  $U_{s\beta}$  - components longitudinal and transverse of the voltage in the stator

$U_{rd}$  and  $U_{rq}$  - components longitudinal and transverse of the voltage in the rotor

$i_{s\alpha}$  and  $i_{s\beta}$  - components longitudinal and transverse of the current in the stator

$i_{rd}$  and  $i_{rq}$  - components longitudinal and transverse of the current in the rotor

$R_s$  and  $R_r$  - active resistances in the stator and in the rotor

$d\Psi_{s\alpha}/dt$  - derivative of the component longitudinal of the flux of the stator

$d\Psi_{s\beta}/dt$  - derivative of the component transverse of the flux of the stator

$d\Psi_{rd}/dt$  - derivative of the component longitudinal of the flux of the rotor

$d\Psi_{rq}/dt$  - derivative of the component transverse of the flux of the rotor

Besides these equations,  $\Psi_s$  and  $\Psi_r$  are described by the system below:

$$(5) \Psi_{s\alpha} = L_s \cdot i_{s\alpha} + L_m \cdot \cos \varphi_{e1} \cdot i_{rd} - L_m \cdot \sin \varphi_{e1} \cdot i_{rq}$$

$$(6) \Psi_{s\beta} = L_s \cdot i_{s\beta} + L_m \cdot \sin \varphi_{e1} \cdot i_{rd} + L_m \cdot \cos \varphi_{e1} \cdot i_{rq}$$

$$(7) \Psi_{rd} = L_m \cdot \cos \varphi_{e1} \cdot i_{s\alpha} + L_m \cdot \sin \varphi_{e1} \cdot i_{s\beta} + L_r \cdot i_{rd}$$

(8)  $\Psi_{rq} = -L_m \cdot \sin \varphi_{e\alpha} \cdot i_{s\alpha} + L_m \cdot \cos \varphi_{e\alpha} \cdot i_{s\beta} + L_r \cdot i_{rq}$ , where  $\varphi_{e\alpha}$  – is the angle between  $\Psi_s$  and  $\Psi_{s\alpha}$

It calculates of (9). [3]

$$(9) \varphi_{e\alpha} = \frac{L_m^2}{(L_s \cdot L_r - L_m^2) \cdot L_s}$$

The electromagnetic torque is defined by expression (10). [1]

$$(10) M_m = Z_p \cdot L_m \cdot (i_{s\beta} \cdot i_{rd} - i_{s\alpha} \cdot i_{rq}) \cdot \cos \varphi_{e\alpha} - (i_{s\beta} \cdot i_{rd} + i_{s\alpha} \cdot i_{rq}) \cdot \sin \varphi_{e\alpha}$$

If it is accepted that the system is completely symmetric, then by measuring the voltages and the currents in two of the phases supply, all those unknowns that we spoke at the beginning can be obtained. For that purpose, from the known voltages and currents it is possible to calculate the similar from the phase of the third. After that, the supply transforms in two-phase co-ordinate system by means of equations (11) and (12). [1]

$$(11) X_{1\alpha} = \sqrt{\frac{2}{3}} (X_{1a} - \frac{1}{2} X_{1b} - \frac{1}{2} X_{1c})$$

$$(12) X_{1\beta} = \sqrt{\frac{2}{3}} (\frac{\sqrt{3}}{2} X_{1b} - \frac{\sqrt{3}}{2} X_{1c}),$$

where a, b and c are the three phases.

In substituent values of  $U_{s\alpha}$ ,  $U_{s\beta}$ ,  $I_{s\alpha}$  and  $I_{s\beta}$  in (1) and (2), it is possible to find  $d\Psi_{s\alpha}/dt$  and  $d\Psi_{s\beta}/dt$ .

After integrating the two parts separately, come out  $\Psi_{s\alpha}$  and  $\Psi_{s\beta}$ . In this way expression (13) defines the absolute value of the flux of the stator :

$$(13) |\Psi_s| = \sqrt{\Psi_{s\alpha}^2 + \Psi_{s\beta}^2}$$

Then from expression (5) defines  $I_{rq}$  and becomes (14):

$$(14) i_{rq} = \frac{L_s \cdot i_{s\alpha} + L_m \cdot \cos \varphi_{e\alpha} \cdot i_{rd} - \Psi_{s\alpha}}{L_m \cdot \sin \varphi_{e\alpha}}$$

In substituent (14) in (6) obtains (15):

$$(15) i_{rd} = \frac{\sin \varphi_{e\alpha} (\Psi_{s\beta} - L_s \cdot i_{s\beta}) + \cos \varphi_{e\alpha} (\Psi_{s\alpha} - L_s \cdot i_{s\alpha})}{L_m}$$

After combining of (14) and (15), and simplifying the expression,  $i_{rq}$  receives the following:

$$(16) i_{rq} = \frac{\sin \varphi_{e\alpha} (L_s \cdot i_{s\alpha} - \Psi_{s\alpha}) - \cos \varphi_{e\alpha} (L_s \cdot i_{s\beta} - \Psi_{s\beta})}{L_m}$$

On the base of the values of  $i_{s\alpha}$ ,  $i_{s\beta}$ ,  $i_{rd}$  and  $i_{rq}$ , it can be obtained  $\Psi_{rd}$  and  $\Psi_{rq}$  from (17) and (18):

$$(17) \Psi_{rd} = L_m \cdot (\cos \varphi_{e\alpha} \cdot i_{s\alpha} + \sin \varphi_{e\alpha} \cdot i_{s\beta}) + \cos \varphi_{e\alpha} \cdot \sin \varphi_{e\alpha} \cdot (\Psi_{s\beta} - L_s \cdot i_{s\beta}) + \cos^2 \varphi_{e\alpha} (\Psi_{s\alpha} - L_s \cdot i_{s\alpha})$$

$$\Psi_{rq} = L_m (\cos \varphi_{e\alpha} i_{s\beta} - \sin \varphi_{e\alpha} i_{s\alpha}) +$$

$$(18) \quad + \frac{L_r}{L_m} [(\sin \varphi_{e\alpha} (L_s i_{s\alpha} - \Psi_{s\alpha}) - \cos \varphi_{e\alpha} (L_s i_{s\beta} - \Psi_{s\beta}))]$$

The rotational frequency of the rotor  $\omega_r$  is defined by expression (19)

$$(19) \quad \omega_r = \int \frac{Z_p}{\sum J} (M_m - M_w) dt, \text{ where}$$

$\sum J$  - is the torque general of inertia

$M_w$  - is the torque statical

$M_m$  - is the torque electromagnetic

$Z_p$  - is the number of pairs of poles

On the basis of the explained theory, a model of electrical motor is created. It is shown on fig.1

At the beginning from the measured values of the voltages and currents from two of the phases, are calculated the similar ones in the phase "w". After that, the supply transforms in two phase co-ordinate system. Then by using the values obtained, it is possible to calculate  $d\Psi_{s\alpha}/dt$ ,  $d\Psi_{s\beta}/dt$ ,  $|\Psi_s|$  and all others unknowns.

By knowing  $M_w$ ,  $Z_p$  and  $M_m$  from (20) is defined the sliding - s

$$(20) \quad s = 1 - \frac{n Z_p}{60 f}, \text{ where } f - \text{ is the frequency of the voltage supply}$$

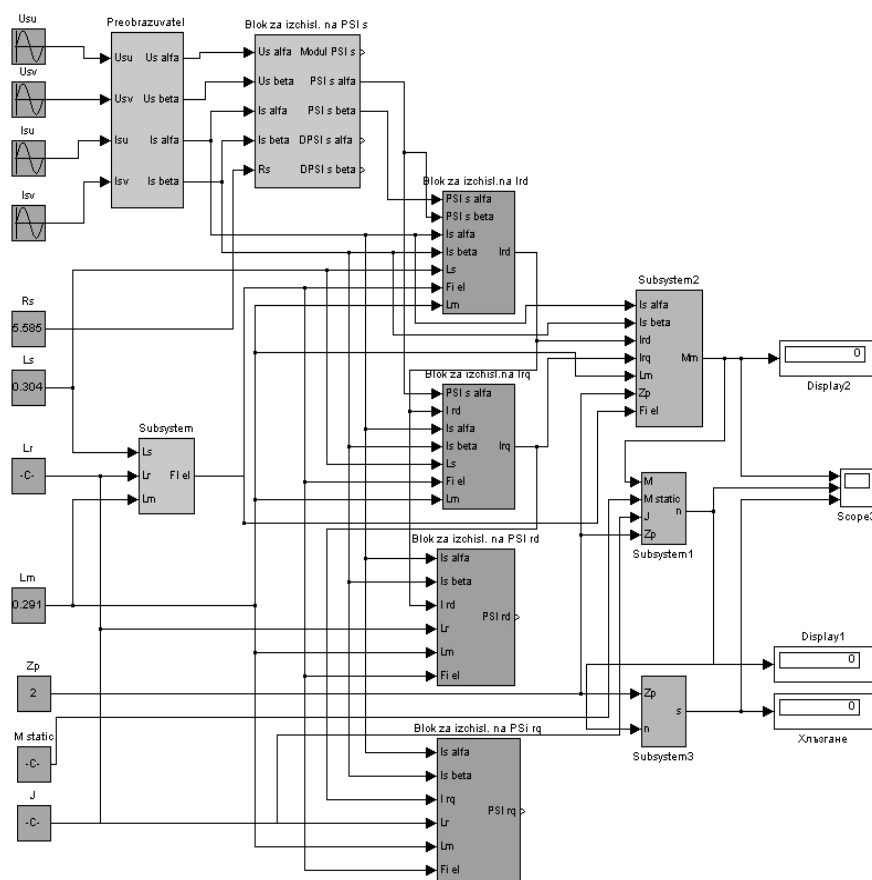


Fig.1. Model of electric motor

The investigations are made with the parameters of real motor. They are shown below:

$P_{\text{nom}} = 1,5\text{kW}$	$L_m = 0,291\text{ H}$
$U_{\text{nom}} = 220\text{V}$	$L_s = 0,304\text{ H}$
$I_{\text{nom}} = 3,8\text{ A}$	$L_r = 0,3066\text{ H}$
$M_m = 10,23\text{ N.m}$	$Z_p = 2$
$J = 0,00278\text{ kg.m}^2$	$n = 1400\text{rpm}$

On the base of data to the top, the results of the investigations with the model are watches below. The simulations are made for 10 sec. The form and the values of voltages and currents are presented on fig.2 and fig.3

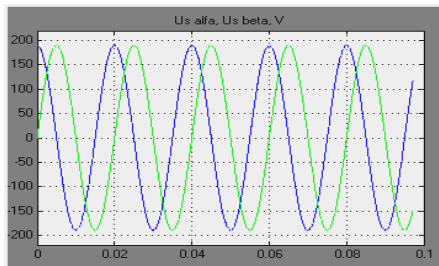


Fig.2.  $\alpha - \beta$  components of the voltage in the stator  $U_s$

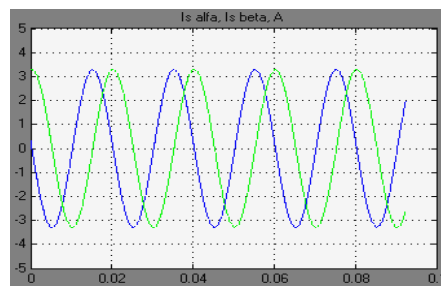


Fig.3  $\alpha - \beta$  components of the current in the stator

For the investigated motor, the components of the current in the rotor  $I_r$  are presented on Fig.4 below:

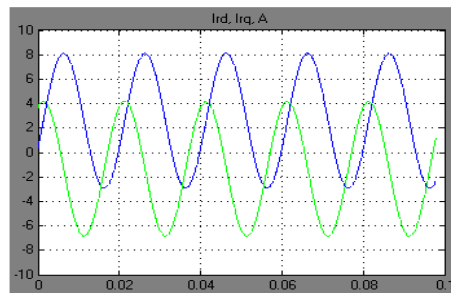


Fig.4 d-q components of the current in the rotor  $I_r$

The mode of the fluxes in the stator and in the rotor is shown in fig.5 and fig.6

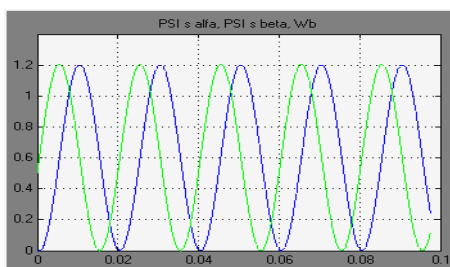


Fig.5  $\alpha - \beta$  components of the flux in the stator

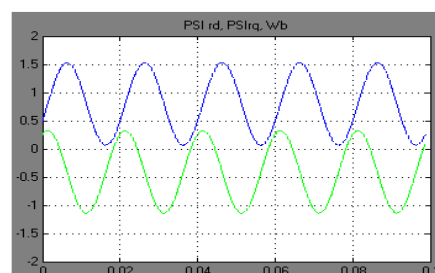


Fig.6 d-q components of the flux in the rotor

The results received from the model are presented on fig. 7 below.

The investigations are made for 10sec by nominal load of the motor. The torque calculated from the model was  $M_m=10,30$  N.m. The torque static in the model was  $M_w=10,12$  N.m. It represents 98% from the torque of the motor  $M_m$ . By this load the revolutions are  $n = 1400$  rpm.

At the beginning it can see that the sliding –  $s$  is 1. For that time  $M_m$  is smaller than  $M_w$ . After the process of transition ( $t = 0,033$ sec. )  $M_m$  becomes bigger than  $M_w$ . From this moment the revolutions become  $n=1399$  rpm and the sliding  $s = 0,067$ .

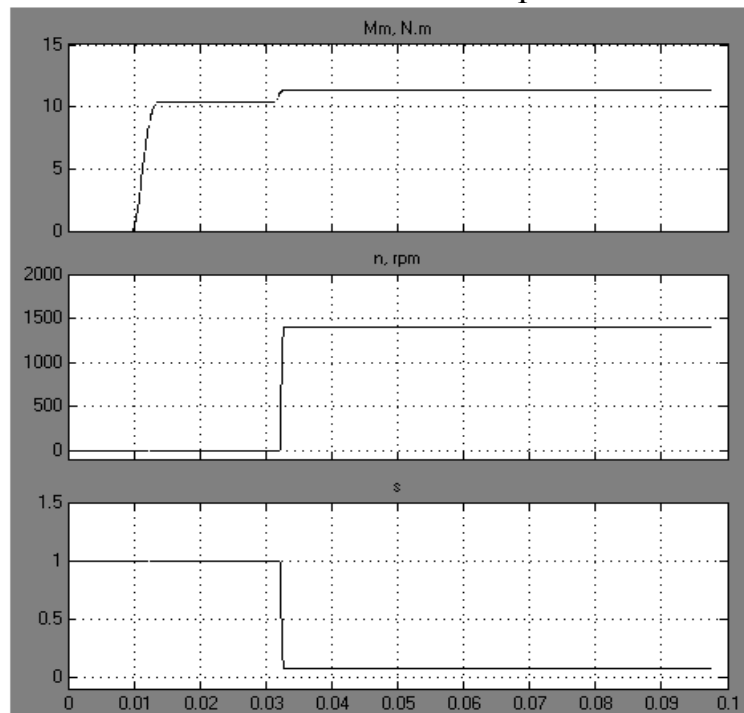


Fig. 7 Results from the investigations

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